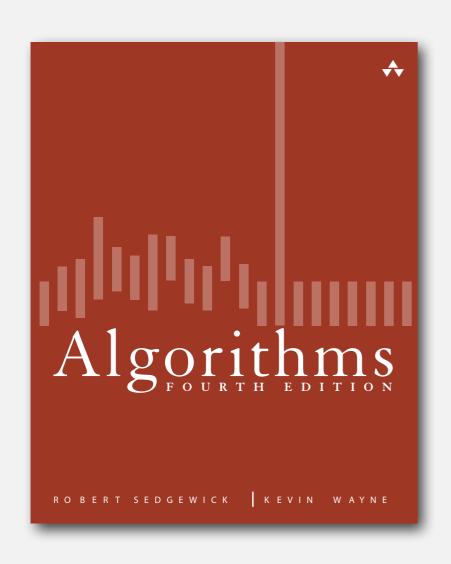
3.1 SYMBOL TABLES



- **API**
- sequential search
- binary search
- ordered operations

► API

- sequential search
- binary search
- ordered operations

Symbol tables

Key-value pair abstraction.

- Insert a value with specified key.
- Given a key, search for the corresponding value.

key

Ex. DNS lookup.

- Insert URL with specified IP address.
- Given URL, find corresponding IP address.

URL	IP address
www.csc.villanova.edu	153.104.202.74
www.princeton.edu	128.112.128.15
www.villanova.edu	153.104.6.101
www.harvard.edu	128.103.060.55
www.simpsons.com	153.104.200.57
<u> </u>	<u> </u>



Symbol table applications

application	purpose of search	key	value
dictionary	find definition	word	definition
book index	find relevant pages	term	list of page numbers
file share	find song to download	name of song	computer ID
financial account	process transactions	account number	transaction details
web search	find relevant web pages	keyword	list of page names
compiler	find properties of variables	variable name	type and value
routing table	route Internet packets	destination	best route
DNS	find IP address given URL	URL	IP address
reverse DNS	find URL given IP address	IP address	URL
genomics	find markers	DNA string	known positions
file system	find file on disk	filename	location on disk

Basic symbol table API

Associative array abstraction. Associate one value with each key.

```
public class ST<Key, Value>
                  ST()
                                                create a symbol table
                                                put key-value pair into the table
           void put(Key key, Value val)
                                                                                          a[key] = val;
                                                (remove key from table if value is null)
                                                value paired with key
                                                                                          a[key]
          Value get(Key key)
                                                (null if key is absent)
           void delete(Key key)
                                                remove key (and its value) from table
       boolean contains(Key key)
                                               is there a value paired with key?
       boolean isEmpty()
                                               is the table empty?
            int size()
                                                number of key-value pairs in the table
Iterable<Key> keys()
                                                all the keys in the table
```

Conventions

- Values are not null.
- Method get() returns null if key not present.
- Method put() overwrites old value with new value.

Intended consequences.

• Easy to implement contains().

```
public boolean contains(Key key)
{ return get(key) != null; }
```

Can implement lazy version of delete().

```
public void delete(Key key)
{  put(key, null); }
```

Keys and values

Value type. Any generic type.

Key type: several natural assumptions.

- Assume keys are Comparable, USE compareTo().
- Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality;
 use hashCode() to scramble key.



Best practices. Use immutable types for symbol table keys.

- Immutable in Java: String, Integer, Double, java.io.File, ...
- Mutable in Java: StringBuilder, java.net.URL, arrays, ...

specify Comparable in API.

ST test client for traces

Build ST by associating value i with i^{th} string from standard input.

```
public static void main(String[] args)
{
   ST<String, Integer> st = new ST<String, Integer>();
   for (int i = 0; !StdIn.isEmpty(); i++)
   {
      String key = StdIn.readString();
      st.put(key, i);
   }
   for (String s : st.keys())
      StdOut.println(s + " " + st.get(s));
}
```

```
keys S E A R C H E X A M P L E values 0 1 2 3 4 5 6 7 8 9 10 11 12
```

output

```
A 8
C 4
E 12
H 5
L 11
M 9
P 10
R 3
S 0
X 7
```

ST test client for analysis

Frequency counter. Read a sequence of strings from standard input and print out one that occurs with highest frequency.

```
% more tinyTale.txt
it was the best of times
it was the worst of times
it was the age of wisdom
it was the age of foolishness
it was the epoch of belief
it was the epoch of incredulity
it was the season of light
it was the season of darkness
it was the spring of hope
it was the winter of despair
                                                       tiny example
% java FrequencyCounter 1 < tinyTale.txt
it. 10
                                                       (60 words, 20 distinct)
                                                       real example
% java FrequencyCounter 8 < tale.txt</pre>
                                                       (135,635 words, 10,769 distinct)
business 122
                                                       real example
% java FrequencyCounter 10 < leipzig1M.txt -
government 24763
                                                       (21,191,455 words, 534,580 distinct)
```

Frequency counter implementation

```
public class FrequencyCounter
   public static void main(String[] args)
      int minlen = Integer.parseInt(args[0]);
      ST<String, Integer> st = new ST<String, Integer>();
                                                                            create ST
      while (!StdIn.isEmpty())
         String word = StdIn.readString();
                                                     ignore short strings
          if (word.length() < minlen) continue;</pre>
                                                                            read string and
                                                                            update frequency
          if (!st.contains(word)) st.put(word, 1);
                                    st.put(word, st.get(word) + 1);
         else
      String max = "";
      st.put(max, 0);
                                                                            print a string
      for (String word : st.keys())
                                                                            with max freq
          if (st.get(word) > st.get(max))
             max = word;
      StdOut.println(max + " " + st.get(max));
```

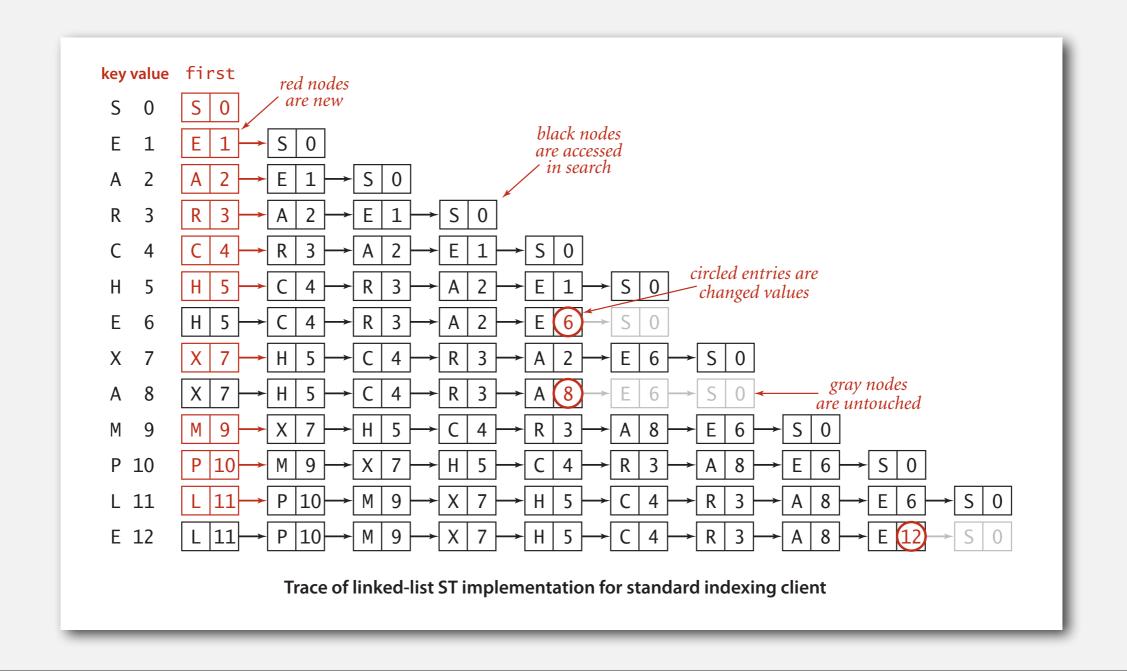
- > API
- sequential search
- binary search
- ordered operations

Sequential search in a linked list

Data structure. Maintain an (unordered) linked list of key-value pairs.

Search. Scan through all keys until find a match.

Insert. Scan through all keys until find a match; if no match add to front.

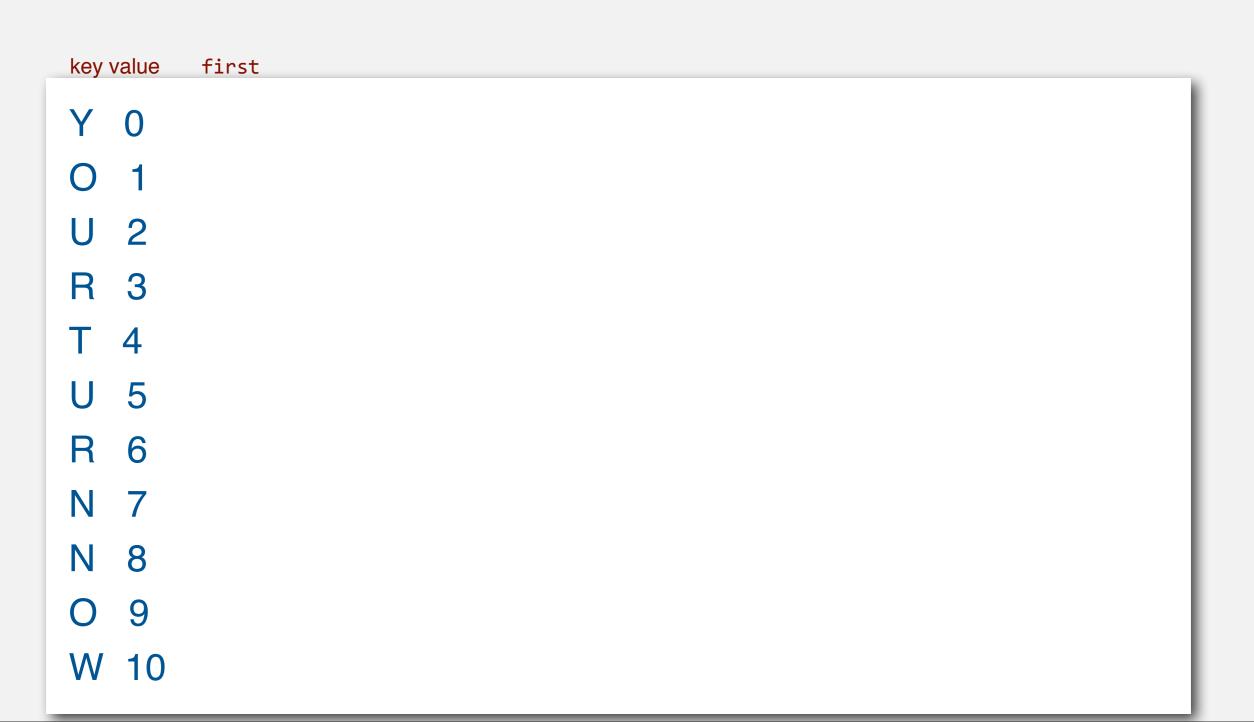


Sequential search in a linked list - Another Example

Data structure. Maintain an (unordered) linked list of key-value pairs.

Search. Scan through all keys until find a match.

Insert. Scan through all keys until find a match; if no match add to front.



Elementary ST implementations: summary

ST implementation	worst-ca (after N			ige case ndom inserts)	ordered iteration?	key interface	
	search	insert	search hit	insert	iteration:	interrace	
sequential search (unordered list)	N	N	N / 2	N	no	equals()	

Challenge. Efficient implementations of both search and insert.

- API
- sequential search
- binary search
- right ordered symbol table ops

Binary search

Data structure. Maintain an ordered array of key-value pairs.

Rank helper function. How many keys < k?

```
keys[]
                      0 1 2 3 4 5 6 7 8 9
successful search for P
        lo hi m
                                                                      entries in black
                                                                      are a [lo..hi]
                                                               entry in red is a [m]
                                                     loop exits with keys[m] = P: return 6
unsuccessful search for Q
       lo hi m
                  loop exits with 10 > hi: return 7
                    Trace of binary search for rank in an ordered array
```

Binary search - Another Example

Data structure. Maintain an ordered array of key-value pairs.

Rank helper function. How many keys < k?

			ke	ys[]				
successful search for R	0	1	2	3	4	5	6	
lo hi m	N	0	R	Т	U	W	Υ	
unsuccessful search for S	0	1	2	3	4	5	6	
lo hi m	N	0	R	Т	U	W	Υ	

Binary search: Java implementation

```
public Value get(Key key)
   if (isEmpty()) return null;
   int i = rank(key);
   if (i < N && keys[i].compareTo(key) == 0) return vals[i];</pre>
   else return null;
private int rank(Key key)
                                            number of keys < key
   int lo = 0, hi = N-1;
   while (lo <= hi)
       int mid = lo + (hi - lo) / 2;
       int cmp = key.compareTo(keys[mid]);
       if (cmp < 0) hi = mid - 1;
       else if (cmp > 0) lo = mid + 1;
       else if (cmp == 0) return mid;
  return lo;
```

Binary search: mathematical analysis

Proposition. Binary search uses $\sim \lg N$ compares to search any array of size N.

Proof Sketch. T(N) = number of compares to binary search in a sorted array of size <math>N.

$$T(N) \le T(\lfloor N/2 \rfloor) + 1$$

left or right half

A recurrence relation => solution: T(N) ~ IgN

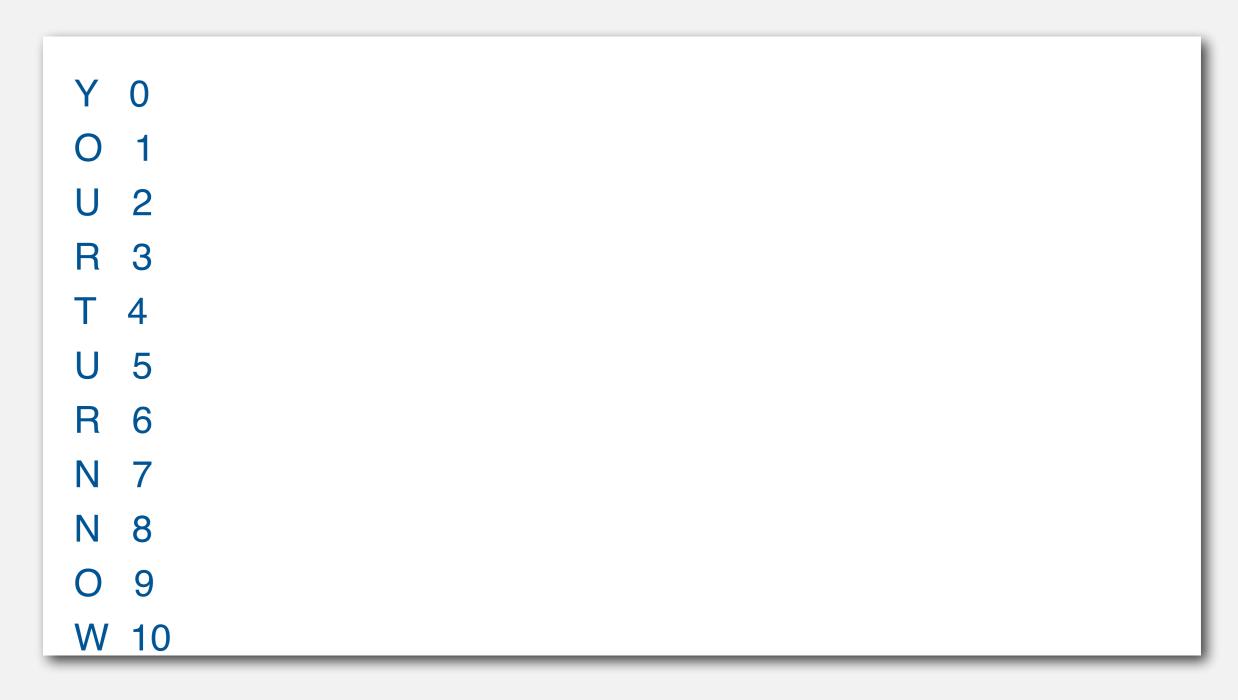
Binary search Inserions: trace of standard indexing client

Problem. To insert, need to shift all greater keys over.

			keys[]									vals[]										
key	value	0	1	2	3	4	5	6	7	8	9	N	0	1	2	3	4	5	6	7	8	9
S	0	S										1	0									
Ε	1	Ε	S			0	ntrie	ec in 1	red			2	1	0					itries wed to			+
Α	2	Α	Ε	S			vere i					3	2	1	0			, 1110	veu i	Tine	rigni	
R	3	Α	Е	R	S							4	2	1	3	0						
C	4	Α	C	Ε	R	S			er	ıtries	in gra	_{iv} 5	2	4	1	3	0					
Н	5	Α	C	Е	Н	R	S				ot mov		2	4	1	5	3	0			entrie ed va	
Ε	6	Α	C	Е	Н	R	S					6	2	4	6	5	3	0	CH	unge	u vu	iues
X	7	Α	C	Е	Н	R	S	X				7	2	4	6	5	3	0	7			
Α	8	Α	C	Е	Н	R	S	X				7	(8)	4	6	5	3	0	7			
M	9	Α	C	Е	Н	M	R	S	Χ			8	8	4	6	5	9	3	0	7		
Р	10	Α	C	Е	Н	\mathbb{M}	P	R	S	Χ		9	8	4	6	5	9	10	3	0	7	
L	11	Α	C	Е	Н	L	M	Р	R	S	Χ	10	8	4	6	5	11	9	10	3	0	7
Ε	12	Α	C	Е	Н	L	M	Р	R	S	X	10	8	4 (12)	5	11	9	10	3	0	7
		Α	C	Ε	Н	L	M	Р	R	S	Χ		8	4	12	5	11	9	10	3	0	7

Binary search: trace of standard indexing client - Another Example

Problem. To insert, need to shift all greater keys over.



Elementary ST implementations: summary

ST implementation	worst-ca (after N			ige case ndom inserts)	ordered iteration?	key interface
	search	insert	insert	iteration:	interrace	
sequential search (unordered list)	N	N	N / 2	N	no	equals()
binary search (ordered array)	log N	N	log N	N / 2	yes	compareTo()

Challenge. Efficient implementations of both search and insert.

- API
- sequential search
- binary search
- ordered operations

Ordered symbol table API

```
keys
                                             values
                     min() \longrightarrow 09:00:00
                                           Chicago
                                            Phoenix
                               09:00:03
                               09:00:13→ Houston
            get(09:00:13)—
                               09:00:59
                                           Chicago
                               09:01:10
                                           Houston
          floor(09:05:00) \longrightarrow 09:03:13
                                            Chicago
                                            Seattle
                               09:10:11
                                           Seattle
                select(7) \longrightarrow 09:10:25
                               09:14:25
                                           Phoenix
                               09:19:32
                                           Chicago
                               09:19:46
                                           Chicago
keys(09:15:00, 09:25:00) \longrightarrow
                               09:21:05
                                           Chicago
                                           Seattle
                               09:22:43
                               09:22:54
                                           Seattle
                               09:25:52
                                           Chicago
        ceiling(09:30:00) \rightarrow 09:35:21
                                           Chicago
                                           Seattle
                               09:36:14
                     max() \longrightarrow 09:37:44
                                            Phoenix
size(09:15:00, 09:25:00) is 5
     rank(09:10:25) is 7
      Examples of ordered symbol-table operations
```

Ordered symbol table API

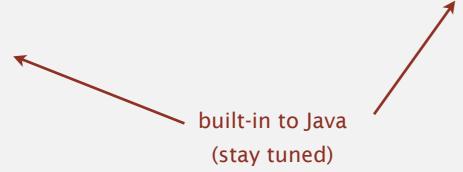
```
public class ST<Key extends Comparable<Key>, Value>
                 ST()
                                                create an ordered symbol table
                                                put key-value pair into the table
           void put(Key key, Value val)
                                                (remove key from table if value is null)
                                                value paired with key
          Value get(Key key)
                                                (null if key is absent)
           void delete(Key key)
                                                remove key (and its value) from table
       boolean contains(Key key)
                                                is there a value paired with key?
       boolean isEmpty()
                                                is the table empty?
            int size()
                                                number of key-value pairs
            Key min()
                                                smallest key
            Key max()
                                                largest key
            Key floor(Key key)
                                                largest key less than or equal to key
            Key ceiling(Key key)
                                                smallest key greater than or equal to key
            int rank(Key key)
                                                number of keys less than key
            Key select(int k)
                                                key of rank k
           void deleteMin()
                                                delete smallest key
           void deleteMax()
                                                delete largest key
            int size(Key lo, Key hi)
                                                number of keys in [lo..hi]
Iterable<Key> keys(Key lo, Key hi)
                                                keys in [lo..hi], in sorted order
Iterable<Key> keys()
                                                all keys in the table, in sorted order
```

Keys and values - Revisited

Value type. Any generic type.

Key type: several natural assumptions.

- Assume keys are Comparable, USE compareTo().
- Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality;
 use hashCode() to scramble key.



Best practices. Use immutable types for symbol table keys.

- Immutable in Java: String, Integer, Double, java.io.File, ...
- Mutable in Java: StringBuilder, java.net.URL, arrays, ...

specify Comparable in API.

Equality test

All Java classes inherit a method equals ().

Java requirements. For any references x, y and z:

```
• Reflexive: x.equals(x) is true.
```

- Symmetric: x.equals(y) iff y.equals(x).
- Transitive: if x.equals(y) and y.equals(z), then x.equals(z).
- Non-null: x.equals(null) iS false.

```
do x and y refer to the same object?
```

Default implementation. (x == y)

Customized implementations. Integer, Double, String, File, URL, ...

User-defined implementations. Some care needed.

Implementing equals for user-defined types

Seems easy.

```
public
             class Date implements Comparable<Date>
   private final int month;
   private final int day;
   private final int year;
   public boolean equals(Date that)
      if (this.day != that.day ) return false;
                                                           check that all significant
      if (this.month != that.month) return false; <
                                                           fields are the same
      if (this.year != that.year ) return false;
      return true;
```

Implementing equals for user-defined types

Seems easy, but requires some care. typically unsafe to use equals () with inheritance (would violate symmetry) public final class Date implements Comparable<Date> private final int month; must be Object. private final int day; Why? Experts still debate. private final int year; public boolean equals(Object y) { optimize for true object equality if (y == this) return true; check for null if (y == null) return false; if (y.getClass() != this.getClass()) objects must be in the same class return false; (religion: getClass() VS. instanceof) Date that = (Date) y; cast is guaranteed to succeed if (this.day != that.day) return false; check that all significant if (this.month != that.month) return false; <</pre> fields are the same if (this.year != that.year) return false; return true;

Equals design

"Standard" recipe for user-defined types.

- Optimization for reference equality.
- Check against null.
- Check that two objects are of the same type and cast.
- Compare each significant field:
 - if field is a primitive type, use ==
 - if field is an object, use equals () apply rule recursively
 - if field is an array, apply to each entry

 or Arrays.deepEquals(a, b),

but not a.equals(b)

Best practices.

- No need to use calculated fields that depend on other fields.
- Compare fields most likely to differ first.
- Make compareTo() Consistent with equals().

```
x.equals(y) if and only if (x.compareTo(y) == 0)
```